



Defence Research and
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Global Path Planning for Unmanned Ground Vehicles

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Defence R&D Canada – Suffield

Technical Memorandum
DRDC Suffield TM 2004-272
December 2004

Canada

| Report Documentation Page | | | | Form Approved OMB No. 0704-0188 | |
|--|------------------------------------|-------------------------------------|----------------------------|--|---------------------------------|
| Public reporting burden for the collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to a penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number. | | | | | |
| 1. REPORT DATE DEC 2004 | | 2. REPORT TYPE | | 3. DATES COVERED - | |
| 4. TITLE AND SUBTITLE Global Path Planning for Unmanned Ground Vehicles (U) | | | | 5a. CONTRACT NUMBER | |
| | | | | 5b. GRANT NUMBER | |
| | | | | 5c. PROGRAM ELEMENT NUMBER | |
| 6. AUTHOR(S) | | | | 5d. PROJECT NUMBER | |
| | | | | 5e. TASK NUMBER | |
| | | | | 5f. WORK UNIT NUMBER | |
| 7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Defence R&D Canada -Suffield,PO Box 4000, Station Main,Medicine Hat, AB,CA,T1A 8K6 | | | | 8. PERFORMING ORGANIZATION REPORT NUMBER | |
| 9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) | | | | 10. SPONSOR/MONITOR'S ACRONYM(S) | |
| | | | | 11. SPONSOR/MONITOR'S REPORT NUMBER(S) | |
| 12. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release; distribution unlimited | | | | | |
| 13. SUPPLEMENTARY NOTES | | | | | |
| 14. ABSTRACT This paper is an overview of high-level path planning methods used in mobile robotics with special emphasis on outdoor planning for unmanned ground vehicles. It surveys all portions of the path planning process including world representation, graph search algorithms, and planning for partially and completely unknown environments. Planning representations such as Cell Decompositions, Roadmaps, and Potential Fields are covered as well as both heuristic and non-heuristic methods of graph search. Specific recently developed and popular algorithms are also investigated such as A*, D*, Potential Fields, Wavefront Planning, Probabilistic Roadmaps and Rapidly Exploring Random Trees. | | | | | |
| 15. SUBJECT TERMS | | | | | |
| 16. SECURITY CLASSIFICATION OF: | | | 17. LIMITATION OF ABSTRACT | 18. NUMBER OF PAGES 58 | 19a. NAME OF RESPONSIBLE PERSON |
| a. REPORT unclassified | b. ABSTRACT unclassified | c. THIS PAGE unclassified | | | |

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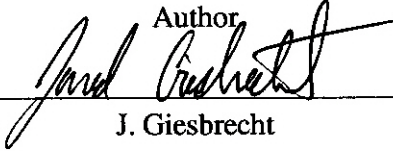
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DRDC Suffield TM 2004-272

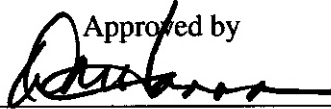
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Abstract

This paper is an overview of high-level path planning methods used in mobile robotics with special emphasis on outdoor planning for unmanned ground vehicles. It surveys all portions of the path planning process including world representation, graph search algorithms, and planning for partially and completely unknown environments. Planning representations such as Cell Decompositions, Roadmaps, and Potential Fields are covered as well as both heuristic and non-heuristic methods of graph search. Specific recently developed and popular algorithms are also investigated such as A*, D*, Potential Fields, Wavefront Planning, Probabilistic Roadmaps and Rapidly Exploring Random Trees.

Résumé

Cet article donne une vue d'ensemble de méthodes de planification de parcours de haut niveau utilisées en robotique mobile axées sur la planification en extérieur pour les véhicules terrestres sans pilote. Il fait l'examen de toutes les étapes de la planification de parcours dont la représentation de l'univers, les algorithmes de recherche par graphes et la planification concernant des milieux partiellement ou complètement inconnus. Les représentations de planification telles que la Décomposition de cellules, le Calendrier de lancement et les Champs potentiels sont couvertes ainsi que les méthodes à la fois heuristiques et non heuristiques de recherche par graphes. Des algorithmes spécifiques récemment mis au point et répandus, tels que A*, D*, Champs potentiels, Planification du front d'onde, Calendriers de lancement probabilistiques et Arbres aléatoires rapides, sont aussi examinés.

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Executive summary

Global path planning is the process of using accumulated sensor data and a priori information to allow an autonomous robot to find the best path to reach a goal position. It is a key component in creating autonomy for unmanned ground vehicles and there are a large number of different techniques currently in use. It is important to have an understanding of the many methods available because each one of them is suited to a specific set of circumstances under which it will be the optimal choice. For this reason, this report surveys the variety of techniques which are currently popular, with special focus on their applicability to outdoor navigation.

A global path planner will often be paired with a local navigator in a typical mobile robot application. Global path planning is concerned with long range planning and is a slow, deliberative process which finds the most efficient path to a long term goal. It is not concerned with vehicle stability or small scale obstacles, which are left to the local navigator system.

The planning process is comprised of two main steps: compiling the available information into an effective and appropriate configuration space and then using a search algorithm to find the best path in that space based on the user's pre-defined criteria such as path distance, proximity to the enemy, and so on. There are three main categories of configuration spaces which have proven to be effective on mobile robots: Cell Decomposition, Roadmaps, and Potential Fields.

The first category of representation, Cell Decomposition, uses a world divided into a set of representative areas, such as regular grid cells, and then describes the characteristics of the world for each of the cells. Typical characteristics represented in the grid are roughness, elevation, traversability and so on. More advanced techniques, such as quadtrees, attempt to be more efficient than regular grids in dividing up the world, to make the path planning process more efficient.

The second type of representation, the Roadmap Methods, attempts to describe the world in terms of how to get from one key location to another, and the cost of getting between them. Road maps are much harder and time consuming to create than Cell Decompositions, but have the advantage of being faster to use once created. Two of the most recent and exciting developments in the field of path planning utilise Roadmaps, Probabilistic Roadmaps and Rapidly Exploring Random Trees.

The third type of representation is called Potential Fields. The robot is represented as an object under the influence of potential created by goals and obstacles in the world much like an electron in an electric field. This method has more commonly been used for local obstacle avoidance in mobile robots but can also make for effective path planning.

Once the world representation has been built using one of the above three methods, the robot then uses a search algorithm to find the best path in that world. Older, less sophisticated algorithms such as Dijkstra's algorithm and Depth-First Search are still in wide use. However, modern developments have led to the use of heuristics, or educated guesses, to speed up the search method. The most popular search algorithm in use, the A* algorithm, is of this type. Further developments, such as the D* algorithm, attempt to speed up the process for circumstances where the world is partially known and new information is frequently being uncovered.

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Sommaire

La planification de parcours global consiste à utiliser les données accumulées par les détecteurs, ce qui à priori est considéré comme information et permet à un robot autonome de trouver le meilleur parcours vers la position désirée. Il s'agit d'un composant clé concernant la création d'autonomie pour les véhicules terrestres sans pilote et un grand nombre de techniques différentes sont actuellement utilisées. Il est important de bien comprendre les nombreuses méthodes disponibles parce que chacune d'entre elle est adaptée à un ensemble de circonstances particulières et représente le choix optimal dans ces circonstances. Pour cette raison, ce rapport examine une variété de techniques qui sont actuellement répandues en focalisant spécialement sur l'applicabilité de ces dernières à la navigation en extérieur.

Le planificateur de parcours global sera souvent jumelé avec un navigateur local durant une application ordinaire de robot mobile. La planification de parcours global se préoccupe de planification à long terme et est un processus lent et délibéré qui trouve le parcours le plus efficace pour un objectif à long terme. Elle ne se préoccupe pas de la stabilité du véhicule ou des obstacles de petite échelle qui sont laissés aux soins du système du navigateur local.

Le processus de planification se compose de deux étapes principales : la compilation de l'information disponible dans un espace d'arrangement efficace et approprié et ensuite l'utilisation d'un algorithme de recherche pour trouver le meilleur parcours dans cet espace en se basant sur les critères prédéfinis par l'utilisateur tel que la distance du parcours, la proximité de l'ennemi et ainsi de suite. Il existe trois catégories principales d'espaces d'arrangement qui ont prouvé être efficaces sur les robots mobiles : la Décomposition de cellules, le Calendrier de lancement et les Champs potentiels.

La première catégorie de représentation, la Décomposition de cellules, utilise un univers divisé en un ensemble de zones représentatives, telles que des cases de grilles ordinaires et décrit ensuite les caractéristiques de cet univers pour chacune des cases. Les caractéristiques ordinaires représentées dans les grilles sont la rugosité, l'altitude, la probabilité de traverser et ainsi de suite. Des techniques plus avancées, telles que les arbres quadratiques, tentent d'être plus efficaces que les grilles ordinaires pour diviser l'univers et rendre plus efficace le processus de planification de parcours.

Le second type de représentation, les méthodes de Calendrier de lancement, tentent de décrire l'univers en termes de comment se rendre d'un lieu clé à un autre et le coût de se rendre entre les deux. La méthode des cartes des routes est plus difficile et plus coûteuse en temps à créer la représentation que le Décomposition de cellules mais cette méthode a l'avantage d'être plus rapide à utiliser une fois la représentation créée. Deux des développements les plus récents et les plus passionnants dans le domaine de la planification de parcours utilisent les méthodes de Calendrier de lancement, Calendriers de lancement probabilistiques et Arbres aléatoires rapides.

Le troisième type de représentation est appelé Champs potentiels. Ce robot est représenté comme un objet soumis à l'influence d'obstacles potentiels, créés sous forme d'objectifs et d'obstacles dans l'univers, d'une manière qui s'apparente beaucoup à celle d'un électron dans un champ électrique. Cette méthode a été utilisée plus couramment pour éviter les obstacles locaux qui se présentent aux robots mobiles mais elle peut aussi être utilisée effectivement dans le domaine de la planification de parcours.

Une fois que la représentation de l'univers a été construite en utilisant une des trois méthodes mentionnées ci-dessus, le robot utilise alors un algorithme de recherche pour trouver le meilleur parcours dans cet univers. Des algorithmes plus anciens et moins sophistiqués tels que l'algorithme Dijkstra et Recherche en profondeur sont encore largement utilisés. Cependant, les développements récents ont amené à utiliser l'heuristique ou des hypothèses bien fondées pour accélérer la méthode de recherche. Un algorithme de recherche de ce type est l'algorithme A* qui est le plus répandu. Des développements plus avancés, tels que l'algorithme D*, tentent d'accélérer le processus dans des circonstances où l'univers est partiellement connu et où l'information nouvelle est fréquemment découverte.

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1. Introduction

A human driver looking at a map of a city, countryside or wilderness can quickly and efficiently decide on the best path to get where he or she is going. Humans can automatically separate portions of the map symbolically in our minds, recognize hazards to our vehicle, roads which will take us there quickly, and effortlessly pick the shortest way to reach our goal. For robots this is not such an easy task owing to their lack of ability to reason symbolically. A robot must first divide up the world into pieces it can recognize as obstacles, undesirable terrain, or dead ends. Then it must systematically search through the world to find the best route.

Through the Autonomous Land Systems initiative, Defence R&D Canada is investigating the area of Unmanned Ground Vehicles (UGVs). The goal is to create autonomous robotic vehicles which can be useful in a wide variety of applications, which can think for themselves and are not a burden to their users. One major challenge is giving vehicles the ability to find their way intelligently through a wide variety of terrains. This may mean finding suitable paths when given a complete map of the area in which the robot is to operate, or perhaps when given nothing more than a suite of sensors to view their world. In some instances it is possible to reach objectives by blindly fumbling toward the goal. However, at other times, systems which are purely reactive will take a long time in reaching their destination if they get there at all. A global world view with the ability to plan well into the future based on accumulated information is a distinct trait of intelligent creatures which allows them to reach goals quicker and avoid potentially dangerous situations. Principles of global path planning therefore need to be applied for successful UGV applications.

This document is a survey of methods that have been developed by the robotics community for path planning by robotic vehicles. The general intention of the survey is to provide guidelines for those methods which are most applicable to outdoor cross country navigation. However, because a great deal of mobile robot research has historically been focused on planning the paths of indoor robots and the movement of robotic manipulators it is important to consider the applicable lessons from that research as well. In addition, a combination of the methods developed for indoor and cross country navigation will probably prove to be effective when implemented for path planning in urban environments.

Autonomous navigation by a UGV or mobile robot from one location to another is a very complex process. The robot must accomplish at least four simultaneous tasks to be successful and efficient:

1. Perception - Viewing the world and interpreting what it sees.
2. Localization - Keeping track of the robot's position.
3. Local Navigation - Making sure the robot doesn't tip, drive into holes or bump into obstacles.

4. Global Path Planning - Finding the fastest and safest way to get from start to goal.

The subject of this survey is the fourth task given above: global path planning which is the process of deliberately deciding on the best way to move the robot from a start location to a goal location. In more technical terms it is defined by Dudek [12] as “determining a path in configuration space between the initial configuration of the robot and a final configuration such that the robot does not collide with obstacles and the planned motion is consistent with the kinematic constraints of the vehicle”. The field of path planning borrows heavily from experience in other fields, such as computer networking, artificial intelligence, computer graphing, and decision making psychology. Although it is not the only type of cognition required, path planning is definitely a key component of autonomous intelligence.

There are a number of terms associated with path planning which are used in different ways by different people. Some are clarified here for the purposes of this report:

Navigation - A very diverse term which can have a variety of meanings. Generally it means “getting from here to there”, but it also encompasses the fields of path planning, motion planning, obstacle avoidance, and localization.

Global Path Planning - Planning which encompasses all of the robot’s acquired knowledge to reach a goal, not just the current sensed world. It is slower, more deliberative, and attempts to plan into the future. There is generally no requirement for it to run in real time, but instead is usually run as a planning phase before the robot begins its journey.

Motion Planning - This term can mean both the high level and low level planning for the way that a robot will move, but must involve a deliberative aspect. This term is used more often in manipulator robotics or for planning on a smaller, more local scale. An example for a mobile robot is the classic parallel parking problem.

Local Navigation - The process of using only the robot’s *current sensed* information of its *immediate* world to avoid obstacles and to ensure vehicle stability and safety. It is much more reactive than path planning and runs in real time. The speed at which a vehicle can travel is limited by the speed at which the local navigator can operate.

Obstacle Avoidance - Used in a very similar manner to local navigation, but where local navigation considers vehicle stability, safety, and goal directedness, obstacle avoidance is concerned with merely getting around objects that are in the robot’s way.

Trajectory Planning - Planning the robot’s next movement. This term is synonymous with motion planning.

Non-holonomic Path Planning - Requires the consideration of constraints which are non-integrable and impose restrictions on possible state transitions. An example is the inability of a car-like robot to move straight sideways.

Kinodynamic Path Planning - Accounts for constraints on the velocity and acceleration that a robot can accomplish.

1.1 Global Path Planning and Local Navigation

It is important not to confuse the tasks of global path planning with local navigation when discussing UGVs. Robust, intelligent systems for outdoor navigation must use both, and these two processes are complementary. The local navigator is a reactive process which relies on the latest sensor data to maintain vehicle safety and stability while moving as fast as possible. Path planning, as discussed here, is a deliberative process that looks ahead to the future and uses information about the world it has been given or accumulated over time to provide a safe path for the robot, prevent it from being stuck in cul-de-sacs, and to reach the goal in the shortest amount of time possible. These are things that a less intelligent, more reactive behaviour cannot accomplish. Unfortunately, it also means that global path planners operate slower and on a much longer time scale than local navigators. Because of this slow planning speed vehicle dynamic concerns are left to the faster, more reactive, local navigator layer. The global planner works at a high level, especially for outdoor robots, due to the scale of barriers in the natural world such as rivers and canyons, while reactive local navigator deals with the smaller sensor-scale obstacles. Sensed obstacles require faster action than the global planner can provide. It must also be noted that path planning is nonsensical for robots that have no ability to store or accumulate information about the environment. In that situation, a local navigation system is all the robot will be able to effectively use.

One of the major issues which much path planning research has focused on is planning with vehicle constraints. Ackerman steered vehicles are commonly used in outdoor environments. The simple fact that they can't move straight sideways greatly complicates the planning problem. Typically, vehicle constraints for global path planning are much more important for indoor vehicles than outdoor vehicles due to the differences in scale of the obstacles and the scale of planned paths between the two environments. For outdoor vehicles the boundary obstacles and cul-de-sacs, etc. tend to be of very large scale with respect to vehicle size. Therefore, for planning purposes, planning is done with the robot treated as a point in space. The maps, or graphs, that are searched through for outdoor path planning consist of a large number of nodes of a smaller size than for indoor application. For these reasons the path planner is slower, and looks further ahead than those planners for indoor robotics. However, for the purpose of this survey, and as a general principle of application for outdoor vehicles, a global path planner will simply plan at a high enough level that the turning radius of the vehicle is small enough to get the vehicle around and out of any obstacles it might find itself in. Because most outdoor environments for UGVs will be relatively uncluttered this often is a valid assumption. We can rely on the fact that the local navigator will handle the low level logistics of moving the robot or that the operator will intervene if the robot does get itself into trouble. However, it must be noted that for many path planning algorithms there is no guarantee that the path planner is competent enough for the environment, and the vehicle may require operator intervention.

| Global Path Planning | Local Navigation |
|--|--|
| Uses accumulated and a priori information | Uses immediate sensor data only |
| Concerned with hills, rivers, canyons, forests, roads, buildings, etc. | Concerned with rocks, holes, slopes, bumps, logs, etc. |
| Plans for long distances and time periods | Plans for immediate vicinity for a short time ahead |
| Slow, deliberative process | Fast and reactive |
| Allows robot to avoid getting trapped | Allows robot to travel safely |
| Plan to reach goal in most efficient manner | Plan to travel as fast as possible |
| Simple model of vehicle (point robot) | Complex vehicle model (dynamics and kinematics) |

Figure 1: Global Path Planning vs. Local Navigation

1.2 Path Planning Concerns

Given an initial position and orientation, as well as a goal position and orientation, a path planner's job is to calculate a path which specifies a continuous sequence of positions and orientations in order to avoid contact with obstacles. It should report failure if no such path exists. Historically, the path planning problem has been studied much less for outdoor vehicles than for indoor vehicles. This may be because outdoor environments are much less cluttered than indoor, but is more likely that the ease of use, size and complexity of indoor mobile robots make them ideal experimental vehicles. This document attempts to analyze the methods presented in terms of effectiveness for outdoor path planning, from which indoor path planning has a great many differences. Indoors, the terrain is flat and vehicle stability can safely be ignored. Obstacles are well defined and regular, and a binary obstacle/no obstacle representation is almost always sufficient. Outdoor environments have some of the following complications:

- The range of obstacles is large, a robot must dodge rocks as well as mountains.
- Vast areas of terrain are often not mapped at high enough resolution for planning.
- Negative obstacles such as ravines, holes, and ditches pose a threat.
- Tipping hazards for robots exist.
- Outdoor areas often contain large areas of sparsely populated terrain, punctuated by cluttered areas.
- Widely varying traversability exists, such as mud, pavement, tall grass, bushes, trees, and rock piles.

Any navigation system for a UGV will need to incorporate all of these concerns in order to be effective. Nevertheless, many methods developed for indoor robots have applicability for outdoor vehicles but would require adaptation for efficient use. For example, a river with a bridge across it will be much larger than a wall with a door in an office, but they represent similar challenges to the robot but on a different scale. In any event, there are many similar characteristics which all path planners have:

Search Space: This represents the possible states, or positions, orientations and conditions of the robot, the world and its objects. A simple example is the x,y coordinates of a vehicle in the Euclidean space. More complex states may involve conditions as complicated as radio signal strength or fuel level.

Actions: A plan must also generate actions, or ways of moving from state to state.

Time: Planning always involves time in some way, even if not explicitly. A planner may include time in such ways as: “at time t the robot will be at point x,y”, or “the path should take the least amount of time possible.” Usually time is represented simply as a sequence of actions: “after Action A is completed the robot will do Action B”.

Initial and Goal States: The plan is the way the robot will get from the initial to the goal state.

Criteria For Planning: The desired characteristics of the “best” plan, such as time, distance, or safety. These are yardsticks by which to optimize plans.

Constraints: Those items which limit the range of plans that can be made, such as maintaining vehicle safety, stealth or the physical limitations of the robot.

Algorithm: This is the method by which the best plan is obtained given the criteria and constraints for planning.

Plan: The sequence of actions to move from the start configuration to the goal configuration.

There are a number of considerations for path planning that will influence the design of the system and criteria by which they are judged:

Environment: Does path planner sufficiently represent the environment? Is the application indoor or outdoor? Is it cluttered or relatively open?

Robot Structure: Does the path planner provide a sufficient but not excessively detailed representation of the vehicle with respect to size and mobility constraints?

Optimality: Requirements can be based on minimum distance traveled, time taken, vehicle safety, etc.

Completeness: Will it find a path if one exists?

Space and Time Complexity: Can it operate fast enough so the robot does not need to stop and think?

Dynamic or Unknown Worlds: Can the path planner deal with changing information or goals?

For some other general information regarding mobile robot path planning see [12][44][33][35] [34].

1.3 Overview of Report

The methods for planning are very closely tied with the world representations used. In order to plan a path for a robot, the world must be represented, in order to define that portion of the world in which can be travelled through (free space), that portion that can't (obstacles), and sometimes that part which can be travelled in, but is undesirable (traversability analysis). Therefore, the first section of this report is all about the various ways that the information about the world can be represented within the robot. It covers topological and metric path planning, the idea of a configuration space, and discrete vs. continuous state spaces. The second section surveys specific representations which have been applied to the path planning problem, such as cell decompositions, road maps and potential fields. Once the world is represented within the robot the path planner will need to search through the representation for the best path to the goal using algorithms such as Depth-First, Breadth-First, and Heuristic searches presented in the third section. The final piece of the path planning problem is using information accumulated from sensors. The final two sections survey these methods, which are the most recently developed and most effective for global path planning in outdoor environments.

This report is a survey of global path planning, not local navigation techniques. It does not cover sensor based motion planning techniques, planning algorithms which plan vehicle action on a local scale, or systems which enable rough terrain mobility. This is not to say that the techniques here do not allow for replanning and the consideration of sensor acquired data but that the main planning function goes on within the space of previously acquired information. This survey also gives little consideration to planning with non-holonomic constraints and kinodynamic planning. This is not to say that the planning algorithms presented below cannot be used on vehicles with these types of constraints, but rather the planning is done at a high enough level and over a long enough time scale that they are unimportant factors.

2. World Representation for Planning

2.1 Topological vs. Metric Path Planning

Humans use two types of navigation and representation: topological navigation and metric navigation. Topological navigation operates on landmarks and identifiable locations such as intersections. Directions are given in terms such as "go to the big tree, turn left and cross the river". Topological methods can go by many other names such as qualitative, route based, or landmark navigation. They express space in terms of connections between identifiable locations such as landmarks and intersections, and are dependent upon perspective of the robot (i.e orientation clues are egocentric). Topological representations cannot be used to generate metric representations even though the reverse is true. The representations are used in a more reactive way and are more robust to localization errors. Unfortunately most of the research in this field has been undertaken for indoor environments where the identifiable nature of objects

enable a vehicle to easily find landmarks. It is more difficult in outdoor environments where a sparsity and lack of uniqueness makes topological cues harder to find. Topological methods may use waypoint navigation, visibility graphs, or voronoi diagrams which are all described below. For some typical examples of topological path planning implemented on indoor robots, see works by Park[48] or Thrun[64].

On the other hand, metric navigation lends itself well to outdoor environments even though it requires more competent localization. Metric methods favor techniques which produce an optimal path and express directions in terms of physical travel, often from a bird's eye view. The map structures are independent of orientation and position of the robot. In metric navigation, directions are given in specific geographic terms with distance and direction, such as "travel at 30 degrees for 300 metres then at 170 degrees for 100 meters". Metric paths are usually described as a set of waypoints or subgoals, defined in the (x, y) coordinate system. Often GPS can provide a global coordinate framework. In addition, metric navigation lends itself very well to computer data representation, and computational search algorithms. The metric methods shown later in this report are potential fields and cell decompositions.

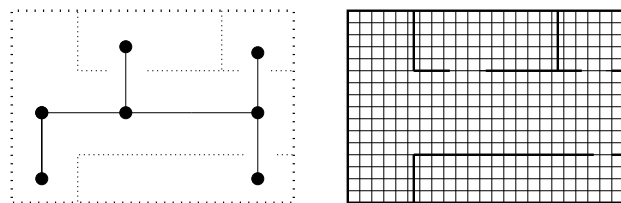


Figure 2: Topological and metric representations.

2.2 Planning Space

2.2.1 Configuration Space

In path planning for mobile robotics, the vehicle and the world through which it travels must both be represented in some manner so that plans can be evaluated in a search space. The search space represents all the possible situations that can exist. In order to plan a robot's motions when there are many degrees of freedom, a construction called a configuration space is used. At every point in time, a robot can have exactly one combination of its position and orientation. This unique combination is called a configuration. A configuration space (c-space) represents each possible configuration as a single point and contains all of the possible configurations of the robot. All of the physical obstacles from the robot's working space are mapped or transformed into this configuration space. This c-space is used where the combination of position and orientation is mapped into a single configuration point, because it transforms the problem from planning complex object motion to planning the motion of a point.

For example, consider a single rigid, wheeled mobile robot, operating in a two dimensional environment. A configuration space which has three dimensions could be used: position x , position y , and orientation angle. Each node in the configuration space will be a unique combination of these three dimensions. If the planning is at a high enough level or if the vehicle is capable of holonomic motion, the configuration space can be reduced to the two dimensional x and y space. For example, if orientation is not a concern, all the positions of a mobile robot could be represented in an (x,y) grid, and the sequence of (x,y) positions the robot will occupy in order to reach the goal then planned. However, what if the world is cluttered, and the vehicle is a car-like robot which has strict conditions of movement for safety, and a limited number of motions it can control? In this case, the vehicle orientation becomes important. Now a larger number of dimensions in the working space (x,y and θ) must be considered, and a configuration space can aid the planning. If planning is done in a three dimensional world then one may have to use up to 6 dimensions in the configuration space (x,y,z positions, as well as roll, pitch and yaw).

A good choice of configuration space will contain the fewest number of dimensions to allow the planning algorithms to work quickly. As degrees of freedom are added for a complex system, the configuration space grows quickly in size and number of dimensions, making planning much more difficult. Unfortunately, as it has been suggested by Latombe [33], the planning problem grows exponentially in time with the number of dimensions in the configuration space. This means that the fewer the number of dimensions that need to be considered the better. For this reason, researchers often use simplifications of the problems to attain faster performance of a path planner. For global path planning, the possible configurations are often reduced to simply the x,y co-ordinate space.

2.2.2 Discrete vs. Continuous Space

In representing the world for robot path planning a continuous or discrete search space can be used. A continuous state space models the world as a continuous set of an infinite number of possible states. Path planning then means finding a continuous trajectory which navigates this space. In general it is more difficult to do planning in a continuous state space, as the mathematics involved become complicated. The continuous state space is more often used for reactive obstacle avoidance rather than for global path planning where the complexities overwhelm its usefulness.

When using a discrete state space the search space is broken up into a finite number of possible discrete states that the vehicle can reside in, and describes any number of characteristics of that state, such as position and pose for vehicles, or elevation, slope, roughness, etc. for an environment's state space.

In order to produce a plan each of these discrete states has a state transition function to determine the other states directly reachable from it. An algorithm explores the state space to find a sequence of states which define a path from the original state to the goal state. This search algorithm may operate on any number of different rules which guide it to find the optimal path based on whatever criteria the designer intends. Another way of thinking of the discrete state space is as a set of nodes with links between them. Links can have costs, and a path is a sequence of nodes connected by links.

This discrete vs. continuous state space consideration can be applied on many levels. For example, if a planner was searching for a steering angle for a vehicle, it could search through a number of discrete candidate steering angles, or it could do a mathematical maximization on the continuous set of all possible steering angles. As another example, potential field methods of path planning can be applied to a continuous field defined by mathematical functions, or the functions can be discretized into a grid map which the path planner searches through.

3. Representation and Path Planning

Most methods of planning use one of three types of configuration space representation, called roadmap, cell decomposition and potential fields. Roadmaps model connections between special points, cell decomposition methods break the world into grids, and potential fields apply mathematical fields to model the world. Of these three methods cell decomposition is the one most widely used for outdoor robotics. Each of these types may be either topological or metric in nature. All the methods mentioned below in general must be discrete, except for the Potential Field method, which can also be implemented in a continuous state space fashion.

3.1 Cell Decomposition Methods

Cell decomposition methods are the most studied and widely applied methods for outdoor robotics. In these methods the planning space is broken up into discrete, non-overlapping regions which are subsets of the c-space and whose union makes up exactly the entire c-space. The result is a graph in which each cell is adjacent to other cells. The methods for traversing from one cell to adjacent cells is called the connectivity graph. A planner then searches through the connectivity graph and the path generated is a sequence of cells the robot should traverse to reach the goal. The cost of traversing a cell may vary and the planner must apply a metric to determine which is the optimal path. Cell decompositions are often used to represent the physical space itself, but can also be used on a configuration space.

3.1.1 Approximate Decomposition

Approximate cell decomposition is created by laying a regular grid over the planning space. The cells of the grid are of a predefined shape and size, and are therefore easy to apply. If there is an object in the area contained by the grid element, that element is marked as an obstacle. Otherwise it is left as free space. The center of each cell becomes a node in the search graph that will be examined to find a path. As shown in Figure 3, these nodes can either be 4-connected or 8-connected representing whether or not the robot is considered to travel diagonally between them. Rather than identifying particular objects or shapes, the cell decomposition simply samples the world and marks up the graph accordingly as to whether the space is full, empty or partially full. Two dimensional binary representations are called bitmaps, and if they have a range of values, occupancy grids. Three dimensional grid elements are known as voxels. This method is called “approximate” because the boundaries of physical objects in the world do not necessarily coincide with the predefined cell boundaries. Approximate cell decomposition is popular for a number of reasons: the algorithms are easier to implement than those for other representations, they are simple to apply to a world space, and they are flexible. The cells size can be tuned for reducing computation time by increasing the cell size, thus reducing the number of cells to search through, or by reducing the cell size to provide more completeness and detail. This makes them appealing for mobile robots where paths must be re-calculated on the fly.

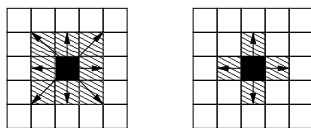


Figure 3: 8-connected and 4-connected grids.

However, there are a few problems with this method despite its ease of use. The first is digitization bias. In cell decomposition methods an obstacle much smaller than the grid size will result in that entire grid square being labelled as occupied. This results in a conservative estimate of the free space, and space that is passable might be considered impassable by the planner. In effect if the grid resolution is too coarse there is no guarantee of finding a path where one exists (i.e. it is non-complete). This problem with approximate cell decomposition is illustrated in Figure 4 to a somewhat exaggerated extent. To combat this a finer scale grid is used, which then means higher storage and calculation costs for path planning. Also, the complexity of these methods grows quickly with the dimension of the c-space so they are realistically applicable only when the c-space has dimensions of around 4 or less. Approximate cell methods were introduced by Brooks and Lozano-Perez [6], and expanded by Zhu and Latombe [70] as well as many, many others since (see the Section 4.0.9 on Trulla and Section 5.4 on D* below for examples).

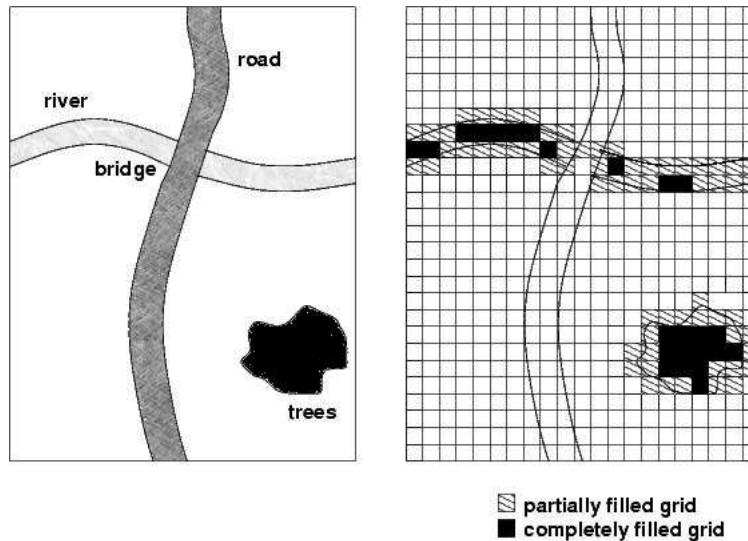


Figure 4: Incompleteness of approximate cell decomposition. The bridge is labelled as blocked because the grid has resolution which is too low. Also note the inefficiency of the regular grid in the open spaces.

When using approximate cell decomposition the system can use one of many types of shapes to divide up the c-space. Regular cell decomposition using square cells seems to be the dominant method of representation for outdoor vehicles. Regular grids have an innate ability to be general, as there are no assumptions about the size and shape of objects inherent in the representation, which is good for outdoor environments.

The cells in the decomposition will have costs associated with traversing them. If this cost is a binary value the map simply contains obstacle and free space regions, which is very common for indoor robotics. However, one can also assign a wider variety of values to the cell cost, resulting in a graph that describes traversability of an area with more flexibility, as outdoor obstacles rarely have easily definable boundaries. For example, to the map cells in a map for an outdoor world one could assign many different costs of traversal, such as roughness, slope, trafficability, etc, which can then be combined to form a total cost value. This flexibility in representation allows for a powerful path planning mechanism.

3.1.2 Adaptive Cell Decomposition

Adaptive cell decomposition is used to reduce the number of cells used in open areas (in order to waste less memory storage space and computation time), and to remove the digitization bias of the regular cell decomposition. It is a good tactic for expansive natural terrains in which there are large areas with the same traversability. Adaptive decomposition relies on the fact that

much of the information in the free space is redundant in a regular cell decomposition. The regular shape of the cells is maintained, but the cells are recursively reduced in size in order to both use the space more efficiently and maintain as much detail as possible. The result is less memory required and less processing time.

The most common type of adaptive decomposition is a quadtree as shown in work by Samet [57] or Naniwa[45]. It begins by imposing a large size cell over the entire planning space. If a grid cell is partially occupied, it is sub-divided into four equal subparts, which are then reapplied to the planning space. These subparts are then subdivided again and again until each of the cells is either entirely full or entirely empty. The resulting map has grid cells of varying size and concentration, but the cell boundaries coincide very closely with the obstacle boundaries. A simple quadtree representation is shown in Figure 5.

Unfortunately, adaptive cell decomposition imposes problems for dynamic environments where the robot is acquiring new data and updating its map based on new obstacles. When this happens, it is necessary for the entire data structure of the map to be completely revamped. There is also some difficulty using quad-trees with continuous cost maps, which are more useful on natural terrain, because you cannot subdivide the world into free and occupied regions. In addition, quad-trees have difficulty in providing near optimal paths and often result in jagged paths. One good solution is framed quad-trees as suggested by Chen [7]. As can be seen by comparing the regular quad-tree in Figure 5 with the framed quadtree in Figure 6, a much better path can be found. However, in high clutter environments framed quad-trees can be less efficient than regular grids, due to the overhead required to keep track of the cell sizes and locations.

3.1.3 Exact Cell Decomposition

Exact cell decomposition attempts to solve some of the problems with regular grids in a different way. The cells do not have a predefined size or shape, but are determined based on the world map and the location and shape of obstacles within it. The cell boundaries correspond exactly with the boundaries in the planning space, and the union of the cells is exactly that of the free space in the world. This makes exact cell decompositions complete in that they will always find a path if one exists, but they will not result in optimal (shortest) paths. Unfortunately, there is no simple rule for how to decompose the space into cells. This method is quite difficult to apply for outdoor environments where obstacles are often poorly defined and of irregular shape. It also does not lend itself well to the use of scales of traversability (as opposed to using binary obstacle and free-space regions). See Schwartz[58], or Avnaim [1] for examples of exact representations. A

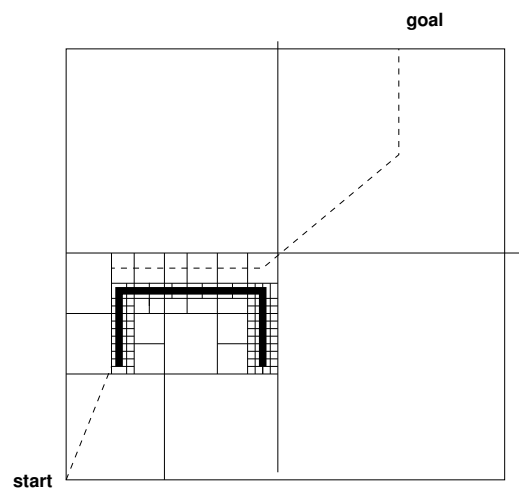


Figure 5: Quadtree representation.

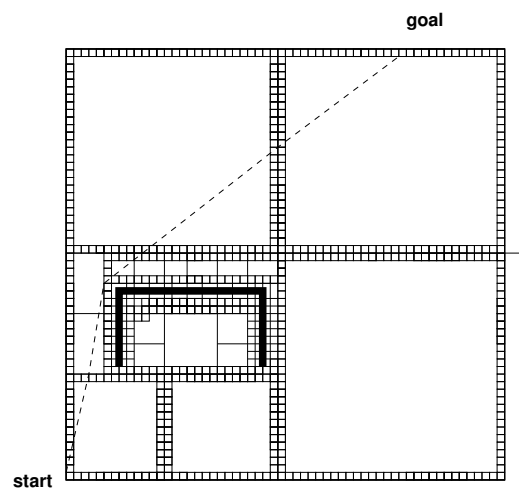


Figure 6: A framed quadtree.

summary of the application of exact cell decomposition for path-planning is given by Sleumer [59]. One type of exact cell decomposition is shown in Figure 7.

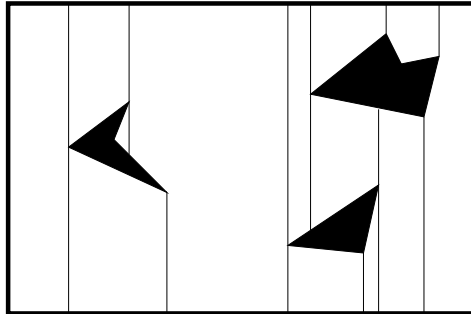


Figure 7: One type of exact cell decomposition.

3.2 Roadmap Methods

The second major type of representation for path planning are the Roadmap Methods. Roadmaps are graphs which represent how to get from one place to another. Roadmap methods of planning find the connections between the robot's free space as a set of one dimensional curves. Once the roadmap has been constructed it is used as a set of standardized paths which the planner will search through to find the optimal solution. The nodes in the graph are usually waypoints that the robot needs to travel between for a successful journey. A topology based road map graph will put the nodes of the graph at distinctive locations which the robot can identify. Roadmaps provide a huge advantage over cell decompositions in the number of nodes a planner needs to search through in order to find a path. The set of nodes doesn't consist of all of the configurations, but a select few that are special. This makes them harder to create, but easier to manipulate and use. On the downside, roadmaps are generally difficult to update or repair as the robot gains new information, because the entire roadmap typically needs to be remade. In addition, most of the methods of creating the graph use artifacts of the map, such as corners of objects or crossroad to generate the landmarks and area boundaries, rather than things that can be sensed by the robot.

3.2.1 Visibility Graphs

One of the earliest roadmap methods, which applies to 2 dimensional c-spaces, is the visibility graph, which was used on Shakey[47]. The visibility roadmap consists of straight line segments which connect the nodes of the polygonal obstacles, without crossing the interior of the obstacles, as in Figure 8. These straight lines make up the paths on which the robot may traverse, and the optimal path is selected by any of a number of search techniques, explained in more detail later in this report. Visibility graph

methods are poor because the calculated paths are tangential to the obstacles and the robot will brush right up against the obstacles. In order to account for this obstacle regions are generally grown to provide a safety margin, although this results in incompleteness and inefficiency of the planner. Another problem is that the obstacles must be clearly defined polygons. This is a problem for outdoor robots because obstacles almost always take on round or amorphous shapes. A simple visibility graph is shown in Figure 8. In this example the possible paths which can be taken by the roadmap are shown in solid lines connecting the corners of the obstacles, and the shortest path through the roadmap, which the robot would take, is shown as the dotted line.

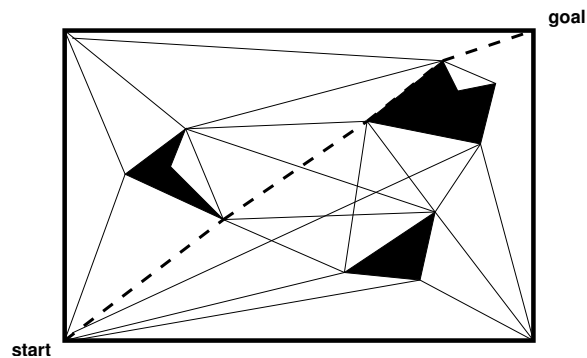


Figure 8: A visibility graph.

3.2.2 Voronoi Diagrams

A voronoi diagram[10] is another popular mechanism for generating a roadmap from a c-space. It can be constructed as the robot enters a new environment. The roadmap consists of paths, or voronoi edges, which are equidistant from all the points in the obstacle region. A rough Voronoi diagram is shown in Figure 9. The points where these edges meet are called vertices, and often have a physical correspondence to aspects of the environment which can be sensed, such as intersections of hallways. In contrast to visibility graphs, Voronoi paths are by definition as far as possible from the obstacles. If a robot follows a voronoi edge, it won't collide with any modeled obstacles, and there is no need to grow obstacle boundaries. This makes Voronoi methods safe, but the paths generated inefficient.

3.2.3 Probabilistic Roadmaps

A much more recent advance in the roadmap methods is the Probabilistic Roadmap (PRM) [22], which attempts to make planning in large or high-dimensional spaces tractable. A PRM is a discrete version of a continuous c-space which contains much fewer states than the original c-space. It is generated by randomly sampling the larger c-space and then

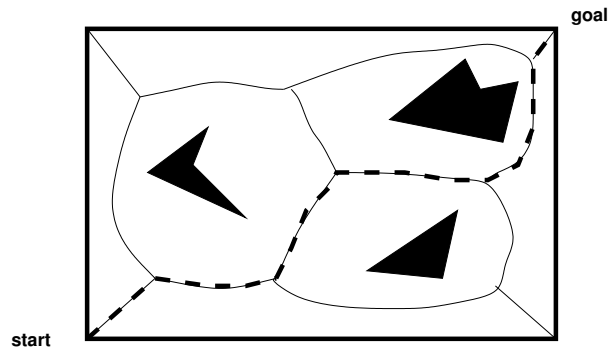


Figure 9: A Voronoi diagram.

connecting those points into a roadmap. PRMs are an improvement because most other planners, especially cell decomposition ones, try to solve the planning problem in the entire search space. PRM methods solve in a roadmap built from a randomly chosen subset of the search space and then use a computationally inexpensive search algorithm to finish the job. PRMs are based on the premise that a relatively small number of points and milestones and paths are usually sufficient to capture the connectivity of free space. This assumption can greatly accelerate the planning process.

Path planning using a PRM has two phases, consisting of a construction of the roadmap phase and path query phase. To construct the map random points in the configuration space are chosen and added to a list of special points. If a point lies in the obstacle region it is discarded. The mapping algorithm attempts to connect this point to a subset of the other configurations already in the list of special randomly chosen points. This connectivity is usually evaluated very simply by using a straight line between the two points, and not connecting them if an obstacle is in the way. This process of random selection and then evaluating connectivity is repeated a large number of times. This creates a list of the available connections between the points that were randomly chosen. This list of connections is the roadmap, which defines a series of waypoints around obstacles in the c-space. In the query phase, when the robot needs to plan a path between two configurations, the algorithm uses the roadmap created in the first phase to search through the waypoint nodes to find the least-cost path between the start and goal configurations. The initial graph building process is computationally expensive, however, once it has been constructed, the search is very efficient. A simple example of a RPM and a path from start to goal is shown in Figure 10.

One problem with a standard PRM method is that it is inefficient for narrow confined spaces. Because the points which make up the roadmap are chosen at random, the chance of catching a random point in the tight space is low, and no connectivity will be established between sections of the map, as shown in

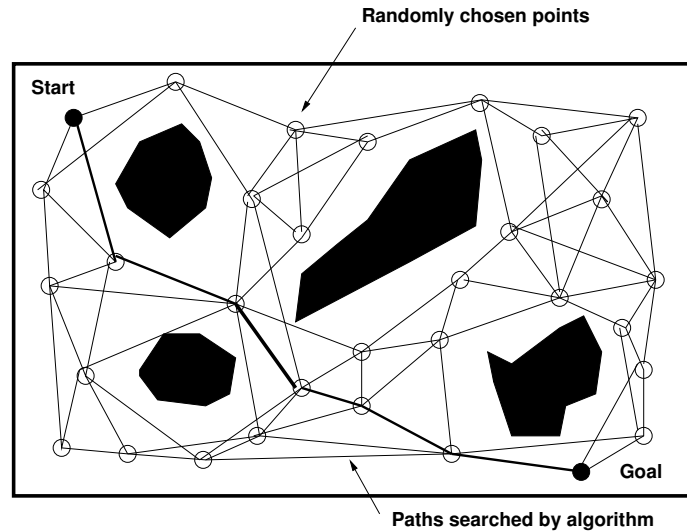


Figure 10: PRM with randomly chosen nodes.

Figure 11. Greater coverage with a greater number of nodes leads to better paths and more chance of getting through tight spots, but makes the planning more complex. This problem has been tackled by Boor[3] and others.

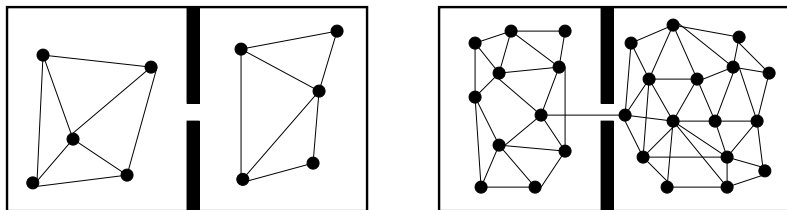


Figure 11: A poorly covered and a well covered PRM.

Another problem with PRMs is that they are usually based on binary obstacles that most other roadmap planners use, rather than a gradual costing. This means that obstacles need to be well defined and generating variable path costs is more difficult than with other methods. A third problem with PRM methods occurs when obstacles are added or removed from the map and the entire roadmap must be regenerated. Because generation of the roadmap is slow and cannot be done in real time, the planner functions poorly when the information is changing often or if the initial information is incorrect. That said, however, the roadmap construction is incremental, and can be expanded as necessary when the robot explores new terrain. Work has been done to alleviate the problems with PRMs by Hsu [19], Leven[38] and others to overcome the dynamic obstacle limitation. There are also many other variations of PRM planners presented in the literature.

3.2.4 Rapidly Exploring Random Trees

A further variation of PRMs is the Rapidly Exploring Random Tree (RRT). Rather than randomly sampling the configuration space as a PRM does the planner begins at the start location and randomly expands a path, or tree, to cover the configuration space. The main focus is to build a roadmap in a fashion which draws the expansion of the connected paths toward the areas which have not been filled up yet. The planner pushes the search tree away from previously constructed vertices. This allows them to rapidly search large, high dimensional spaces. They are also well suited to the capture of dynamic or non-holonomic constraints, which with PRM methods have difficulty (although this capability is not critical for high level global path planning). One method for planning, as shown in Figure 12, is to grow two RRTs, one from the goal and one from the start, and then search for states that are common to both, creating a linked path between the two. For examples, see “Randomized Kinodynamic Planning” by Lavalle [36], and others by Kuffner [32], Cheng[8], and Frazzoli[14].

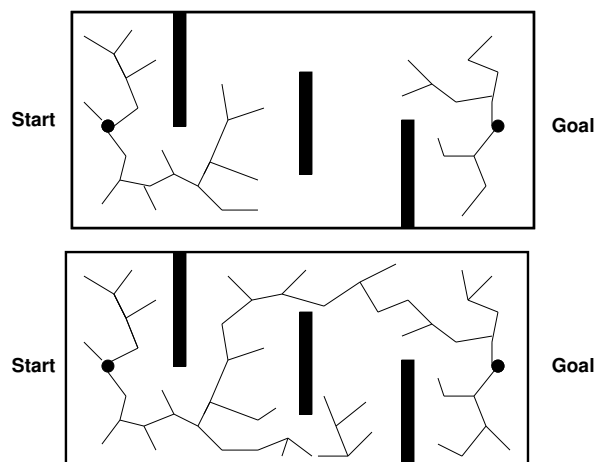


Figure 12: Path planning using RRTs. The roadmap paths are grown in linear increments from both the goal and the start positions. When the two paths grow within a certain distance of one another, they are connected, and the robot can follow the path to reach the goal.

3.3 Potential Fields

Potential Fields is the third major type of representation used in path planning. Potential Field methods are quite different from the previously discussed methods of planning, and have been used extensively in the past. Instead of trying to map the search space they impose a mathematical function over the entire area of robot travel. This method treats the robot as a point under the influence of fields generated by the goals and obstacles in the world, much like an electron in an electric field. Obstacles generate repulsive forces and goals generate attractive forces. These forces are stronger

a) Potential field for Obs1

Obstacles

Start

Goal

Value of potential field due to first obstacle at this point

b) Potential field for Obs2

Start

Goal

c) Potential field for the goal

Start

Goal

d) Sum of potential fields from Obs1, Obs2 and Goal

Start

Goal

Local minima here

Potential fields are often referred to as a local method, as opposed to a global method, because the effect of the field on the robot is almost exclusively based on obstacles near

it. Obstacles far away have little to no effect on the robot's motion, and so it can't be a useful planning method. One simple method of making potential fields a planning method is to forward simulate the motion of the particle in the field, and then use that simulated motion as a planned path. However, there are simpler and more efficient ways to use the potential field for path planning which are described below.

3.3.1 Navigation Functions

The local minima problem can be overcome in one of two ways: 1) by including techniques for escaping minima or 2) with the definition of potential field which has no or few minima. If a potential field that had only one minima was created, then a path from the start to the finish could easily be planned (this is called a global navigation function). There are a very large number of ways to define the potential field, but as was shown by Koditschek[24], it is not possible to create one with no local minima (you will have one saddle point in the field for every obstacle). It is more practical to solve the minima problem by constructing a navigation function, which has a certain small number of equilibrium points (an "almost global navigation function"). These equilibrium points will be unstable so that any small amount of noise will allow the planner to avoid them. This is equivalent to taking solution 1 above (escape the minima). As for solution 2 (making a potential function with few minima), there have been many methods developed. See Koditschek and Rimon [25][54] for examples. However, it is computationally complex to define these navigation functions, and therefore is not that practically useful. Rather than defining these potential functions over free space, it is much easier when the c-space is represented in the form of a grid, such as is done for cell decomposition methods. The potential function over the grid is called a numerical navigation function.

Once more, due to the requirement to discretely model obstacles, potential fields are less useful for outdoor robotics. They are generally more efficient than the graph search methods and don't require an initial processing step to construct the connectivity graph of the configuration space. This makes them useful as a local obstacle avoidance mechanism, due to the ease of calculation once the potential function has been defined. The robot can simply move from one configuration to another by evaluating the resultant vector. As you get more degrees of freedom in the robot and more dimensions in the c-space, it becomes much more difficult for a designer to come up with an appropriate potential function. As a result potential field methods are limited as a planning method and have fallen from favour.

3.3.2 Depth-First Planning and Potential Fields

Using Depth-First planning, a path is iteratively generated as a series of straight path segments through the configuration space[33]. Each segment is

generated from its start point in the direction of the resultant potential field at its start point. The length of the segment will be equal to some predetermined length. The calculation point, or start point, for the next segment is then the end point of the previous segment. The segment length is chosen to be small enough to ensure no collision with obstacles, and that it will not overshoot the goal. This method descends on the steepest part of the potential function until the goal configuration is reached. However, it has problems with local minima where it can easily become trapped.

3.3.3 Best-First Planning and Potential Fields

Best-First search in potential fields[33] retains a wider number of search paths simultaneously, and is more robust to local minima. It involves constructing a tree whose nodes are configurations in the c-space, and whose root is the start position. At every iteration the algorithm evaluates the neighbors in the c-space of those leaves which have the lowest potential value in the field of the configurations investigated so far. The neighbors are then installed in the list of nodes to evaluate with a pointer toward its parent, and the algorithm repeats until the goal is reached. If the most active branch should terminate in a local minimum, another branch will be actively investigated until either it is successful, or the previous branch's local minimum has been overcome (the minimum has been "filled up"). Once the goal has been reached the algorithm follows the backpointers to the start position to define the planned path.

3.3.4 Wavefront Based Planners and Potential Fields

It is possible to create these grid based navigation functions with no minima and plan the path to the goal in one step using a wavefront based planner. The basic idea is that the c-space is considered to be a conductive material, and the wavefront is heat radiating out backward from the goal to the start position. The planner calculates the potential at each node (cell) in the graph as the distance from the goal as it propagates outward. The output of the wavefront propagation is a grid with each location containing the distance to the goal. Once the start position has been reached by this propagation, the planner can step back through those cells with the lowest potential to achieve the path to the goal.

A simplified generic wavefront plan and one possible path are shown in Figure 14. The numbers in the cells represent the cost of any path at that cell, which in this simplified case is the number of cell transitions (distance) to reach the goal. In this example, the influence of the potential field from the obstacles has been omitted for clarity. The effect of including the obstacles' potential fields would be to increase the costs of the cells which border the obstacles.

Two examples of potential fields and wavefront planning are the NF1 and NF2

navigation functions proposed by Latombe and Barraquand [33][2]. This potential field/wavefront method has also been implemented in the Player/Stage environment [15]. A simple illustration of wavefront planning is shown in Figure 14. In this example, the number of transitions from the start to the goal are shown in the grid. The robot could simply follow the decreasing values in order to reach the goal, and could do so along a number of different paths in this example.

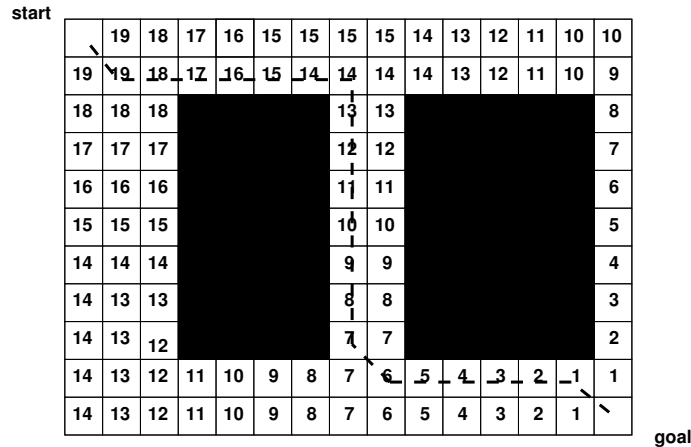


Figure 14: Simplified wavefront planning.

NF1, which was implemented by Lengyel [37], is simple and finds the path with the shortest distance, but has a problem in that it produces paths which graze obstacles. This may be satisfactory if the scale of the plan is high level enough, and you have a local reactive navigator. Brock [5] used NF1 in just this fashion.

NF2 is a similar wavefront propagation technique to NF1, except that it finds paths that are as far away from obstacles as possible, in a similar manner to Voronoi roadmaps. NF2 is more complicated and no longer finds the shortest path to the goal, but gives the robot a larger margin of safety and more room to maneuver. Other wavefront propagation methods include Trulla[42] as described in Section 4.0.9 and Mitchell[41].

4. Graph Search Algorithms

Once a method of representing the environment has been established, it is then necessary to search for the best path through that representation. Graph search algorithms are used with the cell decomposition or roadmap methods of path planning, and also with the potential field methods, as shown in the previous section. These search algorithms come from a wide variety of applications including general problem solving, artificial intelligence, computer networking, and mechanical manipulation.

They systematically search through a graph with the goal of finding a particular node. In the case of mobile robotics they search a roadmap or cell decomposition c-space. The side effect of this search for a particular node, the goal, is that if you keep track of the moves the search algorithm made to find the goal node, you have a path. The simple trick for keeping track of this path is to label each node with its parent node with a backpointer. The string of backpointers defines the path.

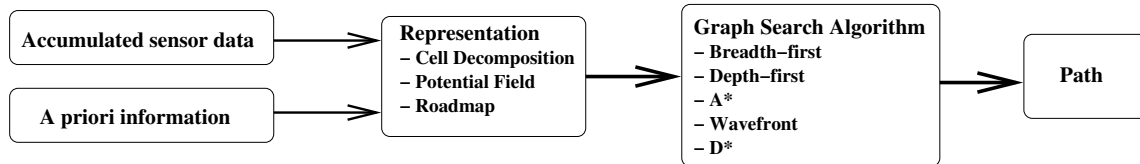


Figure 15: The path planning process.

For UGVs, the search space is usually a two dimensional geographic world map which has been broken into a grid, where the individual states are grid cells, or physical locations in the world map, and the states reachable from any given cell (state) are those immediately surrounding it. The path defined by the algorithm will then be a sequence of grid cells the robot should traverse to reach the goal. Algorithms for UGVs usually attempt to optimize this path based on fewest number of grid cell transitions (as an approximation for distance traveled). As an alternative, a cost can be assigned to traversing each node. In addition to the typical distance metric, many more variables and costs to the planning space can be added. The global space can be marked up with traversability, roughness hazard, slope hazard, boundaries of operation, communication ability, and so on. In this way, the representation is more flexible, intelligent and has more fidelity to the real world. When the paths are evaluated, the path length no longer determined by the number of nodes it has traversed, but by the sum of all the costs of traversals on that path. For example, Saab and VanPutte's system [56] can even evaluate paths based on energy expended going up and down hills.

Many graph search algorithms require that every node in the graph be investigated to determine the best path. This works well when there are a small number of nodes, such as in a Voronoi diagram. However, when planning a path using a regular grid map over a large area this becomes very computationally expensive. Therefore, there are many ways to traverse the graph with many adaptations of two basic themes known as Breadth-First and Depth-First search.

Algorithms are evaluated based on three priorities:

Completeness - Is it guaranteed to find a solution if one exists?

Optimality - Is it guaranteed to find the least cost path?

Time/Space Complexity - What is the time and memory use of the algorithm, as the number of states in the graph increases?

See Russell and Norvig [55] for a more complete description of the following algorithms.

4.0.5 Depth-First Search

Depth-First algorithms search through states trying to move toward the goal as rapidly as possible, continuing on a path until it finds a dead end. This means that it doesn't explore every avenue simultaneously, but rather chooses the avenue which gets it closer to the goal, and only explores that avenue until it is proven successful or unsuccessful. It searches one path to a leaf before following any other path. To use an analogy, if you imagine the graph in terms of a family tree, the first sibling's (node's) descendants are investigated before the descendants of the other siblings. Depth-First algorithms work best for problems where there are many possible solutions, and only one of them is required. At this task, it will operate much faster than a Breadth-First system. Depth-First search can only find the minimum length path by searching through the whole graph, rather than stopping at the first solution. It is the method of choice when there is a known short length to paths but there are a large number of alternatives to sort through.

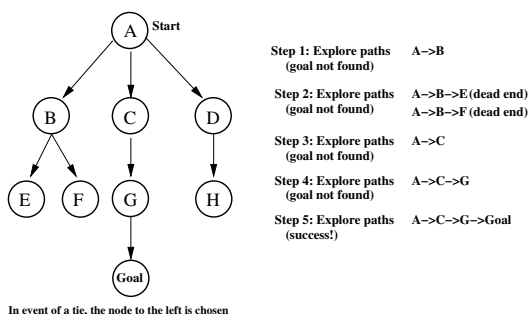


Figure 16: Depth-First Search (note that with Depth-First Search for this example, nodes D and H are never explored).

4.0.6 Breadth-First Search

When searching through the state space, Breadth-First algorithms search all the alternative one-step extensions of the path for their successors before going on to the next step. Every path which has x number of steps is fully explored before examining all those with x +1 steps. Then it advances one step, and examines all the available alternatives again. Breadth-First searches keep all the possible paths to be kept in memory at once, evaluating them simultaneously. To use the same family tree analogy, all the descendants of a certain generation will be investigated before moving on to the next younger generation. Breadth-First algorithms will always find the shortest path on its

first run and are more appropriate when there are a small number of solutions which take a relatively short number of steps.

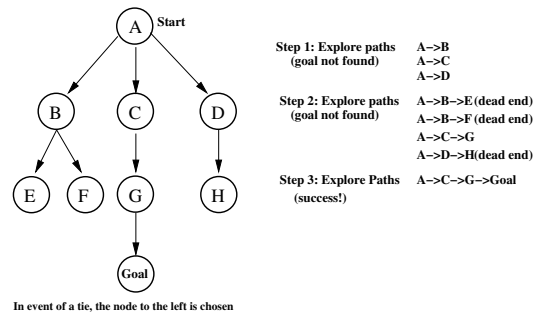


Figure 17: Breadth First Search.

4.0.7 Iterative Deepening

Iterative Deepening search proceeds by a series of depth-bounded Depth-First searches. It may be used to limit storage requirements or to limit the time taken by a Depth-First search. It is much easier to make an iterative deepening algorithm complete (find the guaranteed shortest path) than a Depth-First search, in that you can do so without searching the entire graph space. It is also efficient in that, unlike Breadth-First search, it does not require all paths to be kept in memory at once.

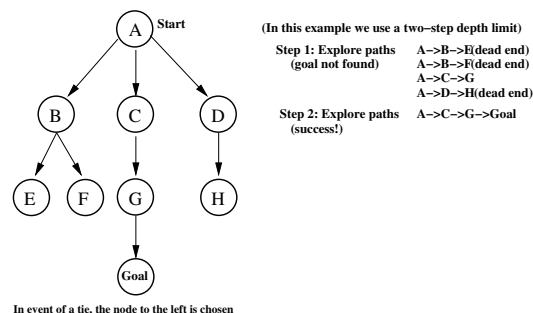


Figure 18: Iterative Deepening Search.

4.0.8 Uniform-Cost Search

A variation of Breadth-First search is Uniform-Cost search, used in graphs with varying costs of traversal. The Uniform-Cost search advances the search at the same cost level, as opposed to advancing the same number of nodes. It turns out that one can find the shortest paths from a given source to all points in a graph in the same time rather than just one point using Dijkstra's algorithm[11], a type of Uniform-Cost search. Dijkstra's algorithm does much

more searching than is necessary, but is guaranteed to find the shortest path. The problem with algorithms given so far is that they often explore an unnecessarily large search area, and take too much time doing so. Thus the use of heuristics is introduced in Section 4.1.

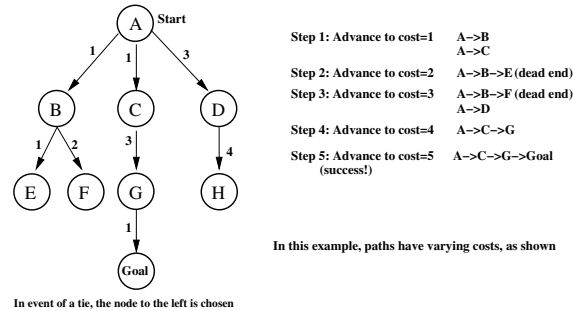


Figure 19: Uniform Cost Search.

4.0.9 Trulla Algorithm

Trulla is a wavefront propagation method of path planning somewhat similar to NF1 and NF2 (described in Section 3.3 under Potential Fields), and is basically a Breadth-First search. It was developed by Hughes [20], and implemented by Murphy in [43] and [42]. It attempts to add two significant improvements to other path planners:

1. Allow dynamic discovery of obstacles and opportunities for navigational savings at the path planning level.
2. Allow terrain characterization with variable costs.

The grid cells for the Trulla planner have a weight representing the difficulty of traversability as well as a non-traversable rating. This representation allows the tradeoff between taking a longer more traversable path and a shorter less traversable path to be handled naturally. The paths in the Trulla algorithm are represented in each grid cell as a vector with direction pointing to the direction to the goal, and the magnitude representing the distance. This is another attractive feature of the algorithm, in that the representation allows an optimal path to the goal to be found from each position in the grid. This is useful if the reactive navigator finds it necessary to deviate from the planned path. A new optimal path can be resumed from the new location without re-running the entire planner, as would be necessary with an algorithm like D* [60]. However, unlike D* when a replan is required, the entire plan must be recomputed.

4.1 Heuristic Search

For many applications, especially for UGVs, the search space, or global map, is very large and has many parts that are unexplored. If there is some additional information which gives the robot an indication of the distance to the goal, a lot of time could be saved. In fact, the time complexity of uninformed search grows exponentially with the size of the problem. In this situation, search algorithms use an heuristic, which is a rule for making a guess as to which path moves us closer to the goal. An evaluation function is used which scores each node or state in the search with an estimate of proximity to the goal. For example, you could use an heuristic which says that the goal is to the south, or perhaps uphill. When the search algorithm evaluates which path to investigate it will choose the one which leads most directly uphill.

4.1.1 Best-First Search

Best-First search [67] is a Depth-First algorithm in which an heuristic indicates how far away each position or state is from the goal. The nodes are evaluated by estimating goodness of a node, comparing it with the goodness of all the other nodes on the frontier, and expand the node which at the moment seems most promising. Unfortunately this may not always be the best choice, but it is the best way to proceed from the search algorithm's point of view. If the metric used to evaluate a node is the distance from the node back to the start then this method is simply a Uniform-Cost search. However, if the metric is an estimate of the distance to the goal, then it is called a Greedy Search. This same Best-First search is used for Potential Field path planning, as described earlier in Section 3.3. In that case, the metric used was the value of the potential field at each node in the search graph. Best-First search makes no guarantee about the shortest path and will, in fact, result in very long paths because it bypasses some branches in the search tree. However, it does do much less searching than other algorithms such as Dijkstra's. Best-First search is not very useful if there is even partial knowledge of the environment, as it is much too greedy and ignores the costs of paths generated.

4.1.2 A* Search

A* is probably the most widely used search algorithm in robotics. It evaluates the goodness of each node as above, but uses a combination of the two metrics to estimate the distance to the goal: distance from the start, like Uniform-Cost search, but also an estimated distance to the goal, like greedy search. It can also be made to be optimal if it is not made too greedy. It was first proposed by Hart [18], and is described in detail in Nilsson [46].

The goodness function for evaluating a path at each node can be expressed as follows: $f(n) = h(n) + g(n)$ where $f(n)$ is the goodness of the node, $h(n)$ is the heuristic value of the node (nearness to the goal), and $g(n)$ is the cost from the

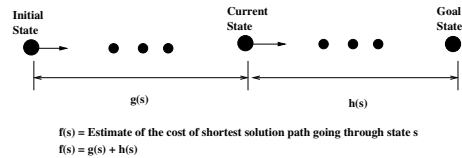


Figure 20: A* Search Algorithm.

start position to the node. As in Best-First search the algorithm will evaluate the node in the graph for which the resultant $f(n)$ is the best. The heuristic estimate, or guess, is often a calculation of what the straight line distance to the goal would be if there were no obstacles.

A* has some very good properties, which is why the algorithm is very commonly used in mobile robotics. Firstly, it will be complete provided that $h(n)$ does not underestimate how close the node is to the goal. Secondly, it is optimal in that it will provide the fastest search of any other shortest path algorithm which uses the same heuristic. A* is a Depth-First algorithm, and it is possible to apply the principle of iterative deepening to it as required. You can adjust the weightings of each of the two factors, $h(n)$ and $g(n)$, with speed and optimality being traded off, which gives A* a lot of flexibility. If the cost to goal weighting is strongest, A* becomes like Dijkstra's algorithm and the result is the optimal shortest path to the goal, but the search process takes longer. If the heuristic weighting is the strongest, A* becomes like Best-First search and shortest paths are given up, but A* will run faster. There are many variations to A* and methods for computing heuristics which may apply to different situations.

5. Path Planning for Partially Known and Unknown Environments

The path planning methods outlined by Latombe[33], and in much of the other early work made the assumption that the world was completely known ahead of time. However, it is quite often that planning is started with information that is incomplete, doesn't have enough resolution, has changed since it was acquired, or is just plain wrong, especially in outdoor environments. This type of planning relies on the free space assumption, which assumes that the unknown world is completely traversable until it is discovered to be otherwise. This means the algorithms need to be adapted to be able to replan based on sensor data that is acquired during the course of the mission. This is not referring to replanning around small scale obstacles, which is left up to the reactive local navigator, but rather replanning because of the acquisition of information which is important to the ability of the robot to reach its goal based on the previous plan. The general method is as follows: the system generates a global path with the

available knowledge and then relies on obstacle avoidance to circumvent obstacles. If the route is completely obstructed or a key piece of information has been found, a replan is required. Action and planning must be interleaved. While the robot is replanning it cannot be moving toward the goal, so it is absolutely crucial that replanning methods are fast, and speed of operation is the driving factor behind their design, sometimes at the expense of optimality and completeness.

5.1 Path Planning for Exploring

Exploration and map-building can be a valuable task for a UGV on a reconnaissance mission. There are many algorithms which enable robots to explore unknown worlds. They can generate optimal behaviour by computing an optimal path to use until a map discrepancy is found, update the map and then replan the entire path. This is problematic in large maps where the replan can be grossly inefficient, especially if there is little information contained within the map and frequent replans are required. Some algorithms sacrifice optimality for fast operation and are concerned with covering the entire area. For a survey of non-heuristic methods, see Rao [53]. Pirzadeh[50] has the robot wander until it discovers the goal. The robot repeatedly moves to the adjacent location with lowest cost and increments the cost of a location each time it visits it in order to penalize repeated trips to the same place. Korf [30] estimates the cost to the goal for each state based on initial information, and updates it with backtracking costs as the robot traverses.

5.2 Path Planning for Partially Known Environments

When operating where there is a partial map available, the intent is to provide more goal directed behaviour than can be provided by exploration algorithms, and speed of planning is still of paramount concern. Lumelsky's bug algorithms[40] move the robot directly toward the goal, assuming there are no obstacles. Once an obstacle is encountered, it moves around it until the point on the obstacle nearest the goal is found, at which time it commences moving directly for the goal. Some other early approaches to planning for partially known environments would rely on a complete replan from scratch when information was found to be incorrect[16]. However, there are much more efficient methods of speeding up the replan task that have been developed since then. Usually, they involve graph search algorithms as presented above which have been refined. Zelinsky [69] increases efficiency by using quad-trees[57] to indicate if a space is traversable or non-traversable. Haigh[17] uses A* search with experience gained in navigating previous terrain to adjust the heuristic used to create a faster search. However, there are other ways of speeding up the search.

Some basic tools which enable faster replanning:

- Heuristics.

- Restricting the planning area using limited look-ahead (Real-time Heuristic Search).
- Replanning only that part of the path affected by changes (Incremental Search).
- Replanning only that part of the path necessary to reach the goal (Incremental Search).

5.2.1 Continuous and Event Driven Replanning

Another key concept involved in planning for partially known environments is that of interleaving planning and execution, or “on-line planning”. The system must manage the amount of time spent on planning and the amount spent executing. There are two different paradigms for triggering replanning: continuous replanning and event driven replanning. Continuous replanning is done every time there is new information from a sensor, at which time it updates all the necessary routes. Unfortunately, this may be too computationally expensive and results in jerky motion if the frequency of replanning is too high. Additionally, continuous planning is highly dependent on sensing quality and is prone to wasting time and effort on phantom obstacles. However, it will be very efficient and opportunistic in sparse environments. The D* algorithm [60] presented in Section 5.4 below is an example of this paradigm.

The alternative is event driven replanning. Some sort of metric is used to judge when it is time to replan. For example, you can use the difference between the intended path and the current path. If either the angle or distance between the two becomes too great, it will call for a replan. This is very good for the case where the real world proves more difficult and has more obstacles than what were originally planned on. Conversely, if there are actually fewer obstacles than planned for, this scheme would miss opportunities to take short cuts. The implementation of the Trulla algorithm given in [42] is an example.

5.3 Real-Time Heuristic Search

Real-Time Heuristic search is a term coined by Korf [30] which includes agent centered search and limited look-ahead search. This method restricts the planning activity to the area around the robot, executes those local actions, and then repeats the planning phase from the new location. Planning is done sequentially to create a global plan. Time is saved by not planning on future contingencies that may never occur. They allow fine grained control over how much planning is performed and try to reduce the sum of the planning time and the plan-execution time of traditional search methods. This method amounts to constructing global path planning as a sum of many local planning activities, as is shown in Figure 21. Some examples are presented by Korf (Learning Real-Time A*[31]), Pemberton [49] and Koenig[27]. Although not explicitly

intended as an agent centered search, the VFH* system developed by Ulrich[66], which uses a local obstacle avoidance system in conjunction with a limited look-ahead A* search, adopts many of the principles of agent centered search. Another implementation by Chin[9] uses a wavefront planner with limited look ahead to plan paths. A good overview of this topic is presented by Koenig [26]. It should be noted that the term “incremental search” is sometimes used for real-time heuristic search, but should not be confused with the term as presented in the next section.

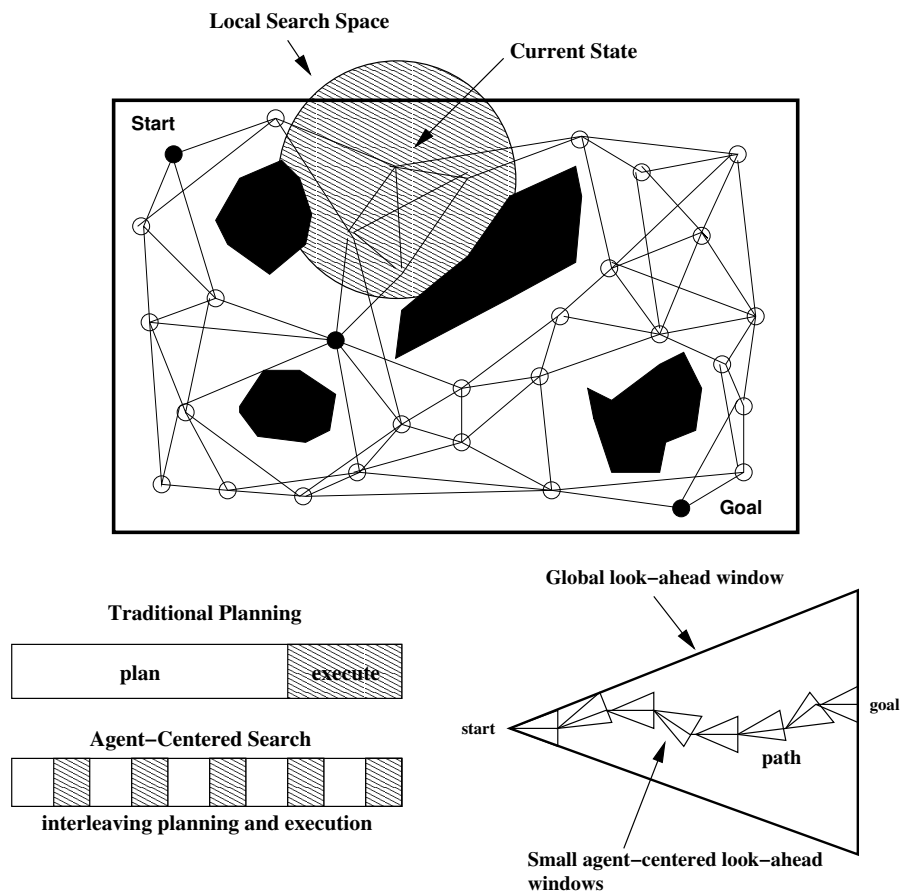


Figure 21: Agent-Centered Search.

5.4 Incremental Heuristic Search

Incremental Replanning, also known as Greedy On-Line Planning or Fast Replanning, replans only that part of the route which is necessary and reuses the information from previous searches as much as possible to increase the speed of operation. Most of the methods developed are versions of heuristic search methods which have been modified.

Incremental Replanning is important for 3 reasons:

- Sensor range is limited, meaning that changes to the robot's information will only need to be patched locally.
- Most obstructions are local in scale and, therefore, will not require a global replan.
- Only that portion of the path remaining between the robot and the goal needs to be replanned (you don't need to replan portions you've already covered).

Earlier approaches started with a map of optimal costs, and when new information was discovered only the affected part of the map was updated. Boulton is an early attempt using polygonal obstacles and binary traversal costs[4]. This was further developed by Travnitzky[65] and Ramalingam and Reps [52] to include a range of traversal costs.

Unfortunately, when the robot is near the goal, these methods are still inefficient because the user probably does not care about updating all of the changes, only those between the robot and the goal. Therefore, a further development was the combination of this incremental search with heuristic search methods to provide a very rapid replanner. Heuristic searches, as shown above, use approximations to estimate the distance to the goal and focus the search to those paths that are relevant. When combined with the speed of incremental methods which don't search from scratch but reuse information, the methods are very rapid and powerful. Other than the algorithms presented below, there are many others, such as [13, 21, 51, 63]. For an overview of incremental search methods see Koenig[29].

The first, and still the most popular of the incremental methods, which was a major advance in path planning for mobile robots, was the D* algorithm from Stentz[60]. It is functionally equivalent to planning from scratch, but much quicker. It can be fast because the impact of sensor acquired data must be local, because of the sensor's limited range, and the method therefore needs to only patch the locally affected portion of the plan. To begin, D* uses whatever a priori information it has to do an A* search from every possible location to the goal. This is computationally expensive, but is done only once at the start. Normally, A* computes only one path, but D* computes all paths at the start. This means that it is easy to switch to a different path and is similar to Trulla in this sense. D* then continuously updates the map and dynamically repair the A* paths affected by the change in the map.

The benefits of D* really come into play when the number of states gets large (i.e. 10^4 , 10^5 , 10^6), and it can offer a one or two order of magnitude improvement over doing complete replans with A*. Because of this, it is more commonly implemented for the more expansive outdoor environments.

There have been a large number of variants of D* presented since its development. The first refinement, Focussed D*[61], uses an heuristic to limit the number of cells which need to be included in replanning, and therefore further reduces the computation time of D*. For better performance in expansive and uncluttered worlds, it was further refined into Framed Quadtree D* by Yahja[68], which uses a more efficient representation to further reduce the computational complexity and memory requirements of the algorithm.

D* Lite[28], an alternative to Focussed D* developed by Sven Koenig, is not based upon the D* algorithm at all but rather his own Lifelong Planning A*. It generalizes A* as well as Ramalingam and Rep's Dynamic SWSF-FP [52], combining techniques to operate faster. It shares many of the advantages of LPA* such as being easier to understand, analyze, optimize and extend than D*, has stronger theoretical foundations, and has been shown to be at least as efficient.

The newest version is Constrained D* (CD*) from Stentz [62]. It is similar to earlier constrained path planners such as ABC[39], in that it plans under constraints, but incorporates the benefits of replanning from D*. It is geared directly for UGVs, and expands D* to use hard and soft objectives. Hard objectives must be met, such as get to the objective by a certain time. Soft objectives, such as maintaining stealth while proceeding to the goal, are met as much as possible while meeting the hard objectives.

6. Time Complexity of Search Methods

In order to use global path planners effectively in mobile robotics, it is important that the graph search process should take as little time as necessary. This is especially true if the system may change goal locations during the mission or if the robot is discovering a lot of new information as it progresses. Below is a summary of methods which can be used to reduce the search time of the algorithms presented in this report:

1. Reduce the number of nodes in the search tree - Path planning algorithms operate in polynomial time, $O(n^k)$, where n is the number of nodes and k is some positive number. This means that, for any algorithm, if the number of nodes is reduced which are to be searched, the computation time required is shortened. There are number of ways of accomplishing this:
 - (a) Using topological methods - Topological methods generally will have many fewer nodes in the world map because they select only key locations to include. However, for most applications the difficulty in providing easily recognizable landmarks to navigate by is prohibitive.
 - (b) Reduce the dimensions of the configuration space - If it is not necessary to plan for all the degrees of freedom of a robot great savings can be had. For this reason, many global path planners operate only in the x,y position space. However, for robot motion planning in complex environments, this is not an effective solution.
 - (c) Efficient representation - For sparse environments, storage methods such as quadtrees can reduce the number of locations in the tree by only using as many nodes as are required. However, they become less efficient when used in complex environments. The results in Figure 22 are taken from Yajha's paper on framed-quadtrees path planning[68]. The graph shows that for low complexity worlds, as indicated by the fractal gain on the x-axis, significant time savings can be made .

2. Sacrificing completeness - If the designer is willing to accept an algorithm which may miss a path where one exists, the algorithm can be optimized. This can be done in two basic ways:
 - (a) Reducing search resolution - Approximate grid representations reduce the number search nodes by decreasing resolution of each grid cell. In doing so, it is possible that computational speed is gained but the approximation may obscure an available path.
 - (b) Reducing the search coverage - Probabilistic Roadmaps reduce the number of search nodes, randomly sampling it to use only a subset of the entire world. The greater the number of samples, the closer the planner will be to being complete but the more time it will take to operate.
3. Choosing an efficient algorithm - If the designer knows something about the search problem, a more appropriate algorithm can be used. For example, if it is known that the solution will only consist of a few number of steps, but there are many alternatives, a Breadth-First algorithm would work better than a Depth-First.
4. Sacrifice optimality - If the designer is willing to accept that the algorithm may not find the best path to the goal but will find a path quickly, the search process can be optimized. Heuristic methods are a prime example of this.
5. Update new information efficiently - For many planning applications, especially outdoors, all the information required will not be available beforehand. Therefore, it is necessary to replan efficiently by using a planner like D*. The results shown in Table 1 come from Stentz's D* paper [60]. The calculation times indicated are from a simulation in which paths were planned initially and then replanned upon the discovery of new information. The improvements that can be had when comparing D* to the A* planner, which does not efficiently replan, can be seen.

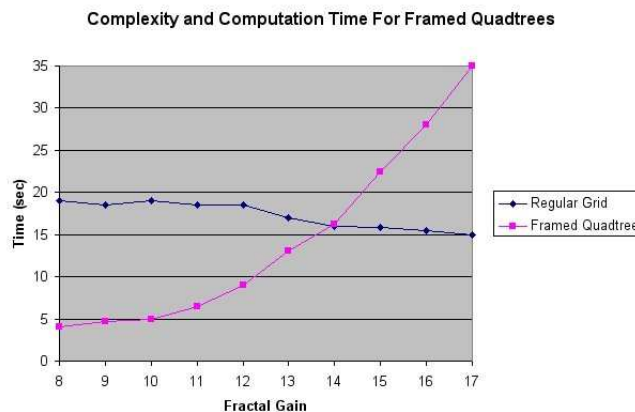


Figure 22: Results for Framed Quadtree Representation.

| Algorithm/Grid Cells | 10^3 | 10^4 | 10^5 | 10^6 |
|-------------------------|----------|-----------|-----------|-----------|
| A* replan from scratch | .427 sec | 14.45 sec | 10.86 min | 50.82 min |
| D* efficient replanning | .261 sec | 1.69 sec | 10.93 sec | 16.83 sec |

Table 1: Results for D* Replanning.

7. Conclusions

Global path planning is an important tool in creating autonomy for UGVs. In certain uncomplicated environments or where a human operator is willing to plan and intervene for the robot regularly, global path planning is not a necessity. However, if the intention is to create a higher level of autonomy in machines, it is a crucial technology. A path planning algorithm can be faster and create better paths than a human planner, especially in cluttered, complex environments.

This report has surveyed a large number of different methods not for historical reasons, but because all of them are still in active use on robot platforms. Due to the multitude of path planners developed so far, one must choose to tailor the path planning method to the application. The designer chooses between them based on such criteria as speed of operation, ability to find the shortest path, and applicability to the scale of obstacles and complexity of the environment. Firstly, one must choose the world representation carefully. For example, if using the right environment and the proper sensing capabilities, a topological roadmap may be appropriate. For expansive, uncluttered working spaces a Framed Quad-Tree may be the correct choice. If you have a large, high dimensional configuration space, Probabilistic Roadmaps and Rapidly Exploring Random Trees are powerful tools. But, if the environment is unknown or changing, these methods are difficult to work with and it may be necessary to use a simple cell decomposition.

Secondly, the graph search algorithm needs to suit the representations and the application. If the speed of planning is not crucial but it is important to find the shortest path, a simple Breadth-First algorithm may do the job. If speed is important, an heuristic algorithm may need to be introduced, such as the A* algorithm. Unfortunately, these algorithms depend on complete knowledge of the world beforehand. If this is not available, a D*-like algorithm will be more appropriate, which would otherwise be much too complex. If the environment is especially cluttered or where there are a great number of contingencies, an Agent Centered search method can be useful where a global look-ahead would be time consuming and wasteful of resources.

Because of the requirement to choose a representation and search algorithm for the environment, it is impossible to say that any one method is better than another, only that it is more appropriate for a given set of circumstances. In any case, there are a wide variety of effective algorithms available to be used for path planning and much research is still being undertaken in refining and improving them. It is certain that global path

planning will be a crucial technology for creating robotic autonomy in the future.

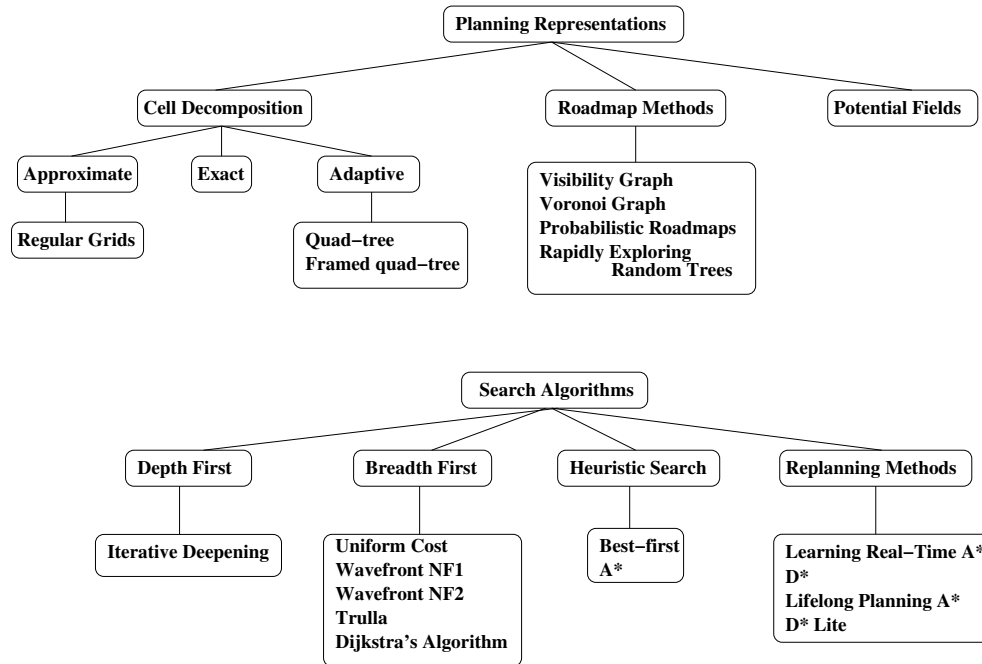


Figure 23: Family Tree of Path Planning Methods

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| 4. AUTHORS (Last name, first name, middle initial. If military, show rank, e.g. Doe, Maj. John E.) Giesbrecht, Jared L. | | |
| 5. DATE OF PUBLICATION (month and year of publication of document) December 2004 | 6a. NO. OF PAGES (total containing information, include Annexes, Appendices, etc) <div style="float: right; font-weight: bold;">54</div> | 6b. NO. OF REFS (total cited in document) <div style="text-align: right; font-weight: bold;">70</div> |
| 7. DESCRIPTIVE NOTES (the category of the document, e.g. technical report, technical note or memorandum. If appropriate, enter the type of report, e.g. interim, progress, summary, annual or final. Give the inclusive dates when a specific reporting period is covered.) Technical Memorandum | | |
| 8. SPONSORING ACTIVITY (the name of the department project office or laboratory sponsoring the research and development. Include the address.) DRDC Suffield | | |
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This paper is an overview of high-level path planning methods used in mobile robotics with special emphasis on outdoor planning for unmanned ground vehicles. It surveys all portions of the path planning process including world representation, graph search algorithms, and planning for partially and completely unknown environments. Planning representations such as Cell Decompositions, Roadmaps, and Potential Fields are covered as well as both heuristic and non-heuristic methods of graph search. Specific recently developed and popular algorithms are also investigated such as A*, D*, Potential Fields, Wavefront Planning, Probabilistic Roadmaps and Rapidly Exploring Random Trees.

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